| Sr.<br>No. | Client Question<br>ID | Question Body and Alternatives   | Marks | Negativ<br>Marks |
|------------|-----------------------|--|-------|------------------|
| Object     | tive Question         |  |       |                  |
|            | 1                     | Let $(y_n)_{n=1}^{\infty}$ be an unbounded sequence of positive terms. Then which of the following statements is TRUE?                               | 4.0   | 1.00             |
|            |                       | $ \begin{array}{ll} \text{Al} & (y_n)_{n=1}^{\infty} \text{diverges to } +\infty. \end{array} $  |       |                  |
|            |                       | A2 $(y_n)_{n=1}^{\infty}$ has a subsequence that diverges to $+\infty$ .   |       |                  |
|            |                       | A3 $(y_n)_{n=1}^{\infty}$ cannot have a convergent subsequence.  |       |                  |
|            |                       | $(y_n)_{n=1}^{\infty}$ must have a convergent subsequence.   |       |                  |
| )bjec1     | tive Question         |  |       |                  |
| 2          | 2                     | Which of the following is TRUE?  | 4.0   | 1.00             |
|            |                       | A1 Every convergent sequence of real numbers is monotone.  |       |                  |
|            |                       | A2 Every monotone sequence of real numbers is convergent.  |       |                  |
|            |                       | A3 Every sequence of real numbers has a bounded subsequence.   |       |                  |
|            |                       | A4 Every Cauchy sequence is bounded.   |       |                  |
|            | tive Question         |  |       |                  |
| 3          | 3                     | The function $f: \mathbb{R} \to \mathbb{R}$ defined as $f(x) = \begin{cases} x^2, & \text{if } x \le 1 \\ 2x - 1, & \text{if } x > 1 \end{cases}$ is | 4.0   | 1.00             |
|            |                       | A1 Continuous at 1 but not differentiable at 1 :   |       |                  |
|            |                       | A2 Differentiable at 1 but not continuous at 1   |       |                  |
|            |                       | A3 : Both continuous and differentiable at 1   |       |                  |
|            |                       | A4 Neither continuous nor differentiable at 1  |       |                  |
|            |                       |  |       |                  |
| )hiect     | tive Question         |  |       |                  |

|                    | Which of the following subsets of $C[0,1] = \{f: [0,1] \to R \mid f \text{ is continuous}\}\ $ are subspaces of $[0,1]$ ?   |     |      |
|--------------------|---|-----|------|
|                    | All The set of all $f \in C[0,1]$ such that $f\left(\frac{1}{3}\right) = 0$ .   |     |      |
|                    | A2 The set of all $f \in C[0,1]$ such that $f\left(\frac{1}{2}\right)$ is a rational number.  |     |      |
|                    | A3 The set of all $f \in C[0,1]$ such that $\int_0^1 f(t)dt = 1$  |     |      |
|                    | The set of all $f \in C[0,1]$ such that $f$ is not differentiable at $\frac{1}{2}$ .  |     |      |
| Objective Question | <u> </u>  |     |      |
| 5 5                | Which of the following is a linearly independent subset of $\mathbb{R}^3$ ?   | 4.0 | 1.00 |
|                    | A1 {(0,1,2),(0,-1,2),(0,0,4) }  |     |      |
|                    | A2 {(0,1,3),(0,1,4),(2,-1,5),(2,6,0) }  |     |      |
|                    | A3 {(0,0,0),(0,1,0),(0,1,1) }   |     |      |
|                    | A4 {(1,0,0),(1,2,0),(1,2,3) }   |     |      |
| Objective Question |   |     |      |
| 6 6                | Consider the Mappings $f, g: \mathbb{R}^2 \to \mathbb{R}^2$ defined as $f(x, y) = (2x + 3y + 1, -x + y)$ and $g(x, y) = (x^2 + y, -x + y)$ . Then,  | 4.0 | 1.00 |
|                    | Both $f$ and $g$ are linear Mappings.   |     |      |
|                    | f is a linear Mapping but $g$ is not.   |     |      |
|                    | g is a linear Mapping but $f$ is not.   |     |      |
|                    | Neither $f$ nor $g$ is a linear Mapping   |     |      |
| Objective Question | <u> </u>  |     |      |
| 7                  | Let $(a_n)_{n=1}^{\infty}$ be sequence given by $a_n = \begin{cases} \left(1 + \frac{1}{n}\right)^n & \text{if } n \text{ is odd} \\ 3 - \frac{1}{n} & \text{if } n \text{ is even} \end{cases}$ . Then | 4.0 | 1.00 |
|                    | $\lim_{n\to\infty} a_n = e \text{ and } \liminf_{n\to\infty} a_n = 3$   |     |      |
|                    | A2  |     |      |

|                    | $\lim \operatorname{Sup}_{n \to \infty} a_n = e \operatorname{liminf}_{n \to \infty} a_n = 1$  |     |      |
|--------------------|--|-----|------|
|                    | $\lim_{n\to\infty} \sup_{n\to\infty} a_n = 3 \lim_{n\to\infty} a_n = 1$  |     |      |
|                    | $\lim_{n\to\infty} \operatorname{Sup}_{n\to\infty} a_n = 3 \operatorname{liminf}_{n\to\infty} a_n = e$   |     |      |
| Objective Question |  |     |      |
| 8 8                | Let $(X,d)$ be any metric space. Which of the following is FALSE?  | 4.0 | 1.00 |
|                    | A1 Every compact subset of $X$ is complete.  |     |      |
|                    | $\frac{A2}{A}$ Every compact subset of $X$ is closed   |     |      |
|                    | A3 Every finite subset of X is both compact and connected.   |     |      |
|                    | A4 Every infinite subset of $X$ has a limit point in $X$ .   |     |      |
| Objective Question |  |     |      |
| 9 9                | If $a_n = \frac{n^2}{n^5 + 1}$ and $b_n = \frac{1}{3^n}$ for all $n \in N$ then  | 4.0 | 1.00 |
|                    | Both $\sum_{n=1}^{\infty} a_n$ and $\sum_{n=1}^{\infty} b_n$ are convergent.   |     |      |
|                    | $\sum_{n=1}^{\infty} a_n$ is convergent but $\sum_{n=1}^{\infty} b_n$ is divergent.  |     |      |
|                    | $\sum_{n=1}^{\infty} a_n$ is divergent but $\sum_{n=1}^{\infty} b_n$ is convergent.  |     |      |
|                    | Both $\sum_{n=1}^{\infty} a_n$ and $\sum_{n=1}^{\infty} b_n$ are divergent.  |     |      |
| Objective Question |  |     |      |
| 10 10              | The number of analytic functions $f: C \to C$ which vanishes at every points on the unit circle $\{z \in C:  Z  = 1\}$ is [where $C$ is the set of all complex numbers.] | 4.0 | 1.00 |
|                    | A1 Infinite  |     |      |
|                    | A2 0   |     |      |
|                    | A3 <sub>1</sub>  |     |      |
|                    | A4 <sub>2</sub>  |     |      |
| Objective Question |  |     |      |

| 11 1     | 11          | Let $W$ be the subspace of $R^3$ given by $W=\{(x,y,z)\in R^3: x+4y+3z=0\}.$ Then $dimW=$        | 4.0 | 1.00 |
|----------|-------------|--|-----|------|
|          |             | A1 0   |     |      |
|          |             | A2 : 1   |     |      |
|          |             | A3 2   |     |      |
|          |             | A4 3 :   |     |      |
| Objectiv | ve Question |  |     |      |
|          | 12          | Which one of the following statements is TRUE?   | 4.0 | 1.00 |
|          |             | A1 A subspace of a connected metric space is connected:  |     |      |
|          |             | A2 : A subspace of a compact metric space is compact   |     |      |
|          |             | A3 A subspace of a complete metric space is complete   |     |      |
|          |             | A4 A subspace of a bounded metric space is bounded:  |     |      |
| Objectiv | ve Question |  |     |      |
|          | 13          | Let $f:R\to R$ and $g:R\to R$ be uniformly continuous mappings. Which of the following is FALSE? | 4.0 | 1.00 |
|          |             | f + g is uniformly continuous on $R$   |     |      |
|          |             | $\stackrel{A2}{:} f - g$ is uniformly continuous on $R$  |     |      |
|          |             | $^{A3}_{:}$ 3f is uniformly continuous on R  |     |      |
|          |             | $^{A4}_{:} fg$ is uniformly continuous on $R$ .  |     |      |
| Objectiv | ve Question | Л  |     |      |
| 14 1     | 14          | The value of $\lim_{x\to 0} \frac{x^{15}-1}{x^{10}-1}$ is  | 4.0 | 1.00 |
|          |             | A1 3/4   |     |      |
|          |             | A2 3/2   |     |      |
|          |             | A3 -3/4  |     |      |

|       |                | A4 -3/2   |     |      |
|-------|----------------|---|-----|------|
|       |                |   |     |      |
|       | ctive Question | WHAT ON OH A C. PATODO  | 4.0 | 1.00 |
| IJ    | 15             | Which of the following statements is FALSE?   | 4.0 | 1.00 |
|       |                | A1 Any subgroup of an abelian group is abelian  |     |      |
|       |                | A2 Any subgroup of an non-abelian group is non-abelian  |     |      |
|       |                | A3 : Any subgroup of a cyclic group is cyclic   |     |      |
|       |                | A4 Any cyclic group is abelian  |     |      |
| Objec | ctive Question |   |     |      |
|       | 16             | The inverse Laplace transform $L^{-1}\left(\frac{s+1}{s^2+2s+2}\right)$ is  | 4.0 | 1.00 |
|       |                | $\stackrel{\text{A1}}{:} e^{-x} \cos x$   |     |      |
|       |                | $\stackrel{A2}{:} e^{-x} \sin x$  |     |      |
|       |                | $\begin{array}{c} A3 \\ \vdots \end{array} e^x \cos x$  |     |      |
|       |                | $\stackrel{A4}{:} e^x \sin x$   |     |      |
| Objec | ctive Question |   |     |      |
|       | 17             | If $A = \left\{ \frac{m+n}{mn} \mid m, n \in N \right\}$ then   | 4.0 | 1.00 |
|       |                | $  ^{A1} lub A = 2 and glb A = 0 $  |     |      |
|       |                | $ ^{A2} lub A = 1 and glb A = \frac{1}{2} $   |     |      |
|       |                | $  ^{A3} lub A = 1 and glb A = 0 $  |     |      |
|       |                | $  ^{A4} lub A = 0 and glb A = 2 $  |     |      |
| Ohiec | ctive Question |   |     |      |
|       | 18             | Consider the linear transformation $T: \mathbb{R}^2 \to \mathbb{R}^3$ defined as  | 4.0 | 1.00 |
|       |                | Consider the linear transformation $T: \mathbb{R}^2 \to \mathbb{R}^3$ defined as $T(x_1, x_2) = (x_1, x_1 + x_2, x_2)$ , then the nullity of $T$ is |     |      |

|       |               | A1 0<br> :  |     |      |
|-------|---------------|---|-----|------|
|       |               | A2 1  |     |      |
|       |               | A3 2 :  |     |      |
|       |               | A4 3  |     |      |
| Objec | tive Question |   |     |      |
| 19    | 19            | The function $f: \mathbb{R} \to \mathbb{R}$ defined as $f(x) = \begin{cases} x^2 \sin \frac{1}{x}, & \text{if } x \neq 0 \\ 0, & \text{if } x = 0 \end{cases}$ is | 4.0 | 1.00 |
|       |               | A1 Continuous at 0 but not differentiable at 0  |     |      |
|       |               | A2 Differentiable at 0 but not continuous at 0  |     |      |
|       |               | A3 Neither differentiable nor continuous at 0   |     |      |
|       |               | A4 Both differentiable and continuous at 0  |     |      |
| Objec | tive Question |   |     |      |
| 20    | 20            | Let $A = \{a, b, c\}$ . Then number of relations containing $(a, b)$ and $(a, c)$ which are reflexive and symmetric but not transitive is                         | 4.0 | 1.00 |
|       |               | A1 1 :  |     |      |
|       |               | A2 2  |     |      |
|       |               | A3 3  |     |      |
|       |               | A4 <sub>4</sub> :   |     |      |
| Objec | tive Question |   |     |      |
| 21    | 21            | Let $A = \{1,2,3\}$ . Then number of equivalence relations containing $(1,2)$ is  | 4.0 | 1.00 |
|       |               | A1 1 :  |     |      |
|       |               |   |     |      |
|       |               | A2 2 :  |     |      |

|       |                | A4 4  |     |      |
|-------|----------------|---|-----|------|
|       |                |   |     |      |
|       | ctive Question |   |     |      |
| 22    | 22             | Which of the following statement is FALSE?                                  | 4.0 | 1.00 |
|       |                | A1 The power set of any countable set is countable.                         |     |      |
|       |                | A2 The Cantor set is uncountable.   |     |      |
|       |                | A3 [0,1]is uncountable.   |     |      |
|       |                | A4 If $X$ and $Y$ are countable sets then $X \times Y$ is countable.        |     |      |
|       | ctive Question |   |     |      |
| 23    | 23             | The radius of convergence of the series $\sum_{n=1}^{\infty} z^{n!}$ Is     | 4.0 | 1.00 |
|       |                | A1 :  |     |      |
|       |                | A2 0  |     |      |
|       |                | A3 <sub>∞</sub> :   |     |      |
|       |                | A4   e  |     |      |
| Ohio  | ctive Question |   |     |      |
|       | 24             | The residue of the function $f(z) = \frac{e^z}{z^2}$ at the pole $z = 0$ is | 4.0 | 1.00 |
|       |                |   |     |      |
|       |                | A2 : 1  |     |      |
|       |                | A3 1/2  |     |      |
|       |                | A4 π<br>:   |     |      |
| Objec | ctive Question |   |     |      |
| 25    | 25             | Which of the following functions is uniformly continuous on $(0,\infty)$ ?  | 4.0 | 1.00 |
|       |                | $ \stackrel{\text{A1}}{:} f(x) = x^2 $                                      |     |      |
|       |                |   |     |      |

|              | $\int_{1}^{A3} h(x) = \sin x$   |     |      |
|--------------|---|-----|------|
|              | $ {}^{A4}_{:} k(x) = (x-1)^2 + 1 $  |     |      |
| bjective Que | stion   |     |      |
| 6 26         | What is $\sum_{k=0}^{n} \binom{n}{k}$ ?                                       | 4.0 | 1.00 |
|              | A1 n!   |     |      |
|              | A2 n <sup>n</sup>   |     |      |
|              | A3 2 <sup>n</sup>   |     |      |
|              | $\begin{bmatrix} A4 \\ : \end{bmatrix}$ $n^2$                                 |     |      |
| bjective Que | stion   |     |      |
| 7 27         | If $\{x_n\}$ converge to $l$ , then   | 4.0 | 1.00 |
|              | $ \stackrel{\text{A1}}{:} \{ x_n \} \text{ converge to }  l . $               |     |      |
|              | $A_{1}^{A_{2}}$ { $ x_{n} $ } will also converge to $l$ .                     |     |      |
|              | A3 $\{ x_n \}$ converge to $l$ , only when $l=0$ .                            |     |      |
|              | $A4 \{ x_n \}$ need not converge.   |     |      |
| bjective Que | stion   |     |      |
| 28           | The limit superior and limit inferior of the sequence $\{x_n = (-1)^n n\}$ is | 4.0 | 1.00 |
|              | $\stackrel{\text{A1}}{:}$ $-\infty$ and -1                                    |     |      |
|              | $^{\mathrm{A2}}_{:}$ -1 and $-\infty$   |     |      |
|              | $A3 - \infty$ and $\infty$ :  |     |      |
|              | $^{\mathrm{A4}}_{:}$ $\infty$ and $-\infty$                                   |     |      |
|              |   |     |      |
| ojective Que | stion   |     |      |

|            | A1 1- 1/2+1/3-1/4+1/5  |     |      |
|------------|--|-----|------|
|            | A2 <sub>1/2-2/3+3/4-4/5+</sub>   |     |      |
|            | A3 <sub>1-1+ 1/2-1/2+1/3-1/3+</sub>  |     |      |
|            | A4 1- 1/1!+1/2!-1/3!+1/4!  |     |      |
| N-i notive | Question   |     |      |
| 30 30      |  | 4.0 | 1.00 |
|            | (i) Rearrangement of series cannot converge to different limits. (ii) Rearrangement of series can converge to at most finite number of limits. (iii) Rearrangement of series can converge to any given real number. (iv) Any rearrangement of absolutely convergent series converge to a unique limit. |     |      |
|            | A1 (iii)   |     |      |
|            | A2 (iv)  |     |      |
|            | A3 (iii) and (iv)  |     |      |
|            | A4 (ii) and (iv)   |     |      |
| Objective  | Question   |     |      |
| 31 31      |  | 4.0 | 1.00 |
|            | A1 Does not exist  |     |      |
|            | A2 Exist and equal to 1  |     |      |
|            | $^{\mathrm{A3}}_{:}$ Exist and equal to $\pi$  |     |      |
|            | A4 Exist and equal to e  |     |      |
| Objective  | Question   |     |      |
| 32 32      |  | 4.0 | 1.00 |
|            | $\stackrel{A1}{:}$ Any real numbers $x$  |     |      |
|            | $\stackrel{A2}{:}$ Only for positive real numbers $x$  |     |      |
|            | A3 Non integer real numbers x  |     |      |

|        |               | $\parallel$ :  |     |      |
|--------|---------------|--|-----|------|
|        |               |  |     |      |
|        |               | $^{\text{A4}}$ Only for negative real numbers $x$  |     |      |
| Object | tive Question |  |     |      |
| 33     | 33            | The function $f: Z \to Z$ , defined by $f(x) = 3x^3 - x$ is  | 4.0 | 1.00 |
|        |               | Al fis bijective   |     |      |
|        |               | f is injective but not surjective  |     |      |
|        |               | $^{\mathrm{A3}}$ f is surjective but not injective   |     |      |
|        |               | $^{\mathrm{A4}}$ f is neither injective nor surjective   |     |      |
| Object | tive Question |  |     |      |
| 34     | 34            | How many numbers in the range 1000-9999 end with 2?  | 4.0 | 1.00 |
|        |               | A1 1000<br>:   |     |      |
|        |               | A2 1200  |     |      |
|        |               | A3 900 :   |     |      |
|        |               | A4 800<br>:  |     |      |
| Obiec  | tive Question |  |     |      |
| 35     | 35            | Let X and Y be sets with  X =100 and  Y =1000. How many bijective functions are there from X to Y?               | 4.0 | 1.00 |
|        |               | A1 100!  |     |      |
|        |               | A2 1000!   |     |      |
|        |               | A3 100000<br>:   |     |      |
|        |               |  |     |      |
| Object | tive Question |  |     |      |
| 36     | 36            | Let X and Y be non-empty sets and f a mapping of X into Y. If A and B are respectively, subsets of X and Y, then | 4.0 | 1.00 |
|        |               | A1 $ff^{-1}(B) \subseteq B$ if and only if f is bijective  |     |      |
|        |               | A2 $ff^{-1}(B) = B$  |     |      |

|      |                | A3 $ff^{-1}(B) = B$ if and only if f is surjective.                                   |     |      |
|------|----------------|---|-----|------|
|      |                | $^{A4}_{:}$ $ff^{-1}(B) = B$ if and only if f is injective                            |     |      |
|      | ctive Question |   |     |      |
| 37   | 37             | Let $f:[a,b] \rightarrow \mathbf{R}$ be a monotonic function. Then                    | 4.0 | 1.00 |
|      |                | Al f is continuous.   |     |      |
|      |                | A2 f is discontinuous at at most two points.  |     |      |
|      |                | A3 f is discontinuous at finitely many points.  |     |      |
|      |                | A4 f is discontinuous at at most countable points.                                    |     |      |
| Obje | ctive Question |   |     |      |
| 38   | 38             | In the real line R, what can one say about non-empty open set?                        | 4.0 | 1.00 |
|      |                | A1 an open interval.  |     |      |
|      |                | A2 the union of a countable disjoint class of open intervals.                         |     |      |
|      |                | A3 the union of a finite class of open intervals.                                     |     |      |
|      |                | A4 none of these.   |     |      |
| Obje | ctive Question |   |     |      |
| 39   | 39             | The sum of the degrees of the vertices of a graph is                                  | 4.0 | 1.00 |
|      |                | A1 the number of edges plus 2   |     |      |
|      |                | A2 the number of vertices minus two   |     |      |
|      |                | A3 two times the number of vertices   |     |      |
|      |                | A4 two times the number of edges  |     |      |
| Obje | ctive Question |   |     |      |
| 40   | 40             | The number of edges of a simple graph with n vertices and with $\omega$ components is | 4.0 | 1.00 |

|       |                | $\begin{vmatrix} A1 \\ \vdots \end{vmatrix} \ge \frac{(n-\omega)(n-\omega+1)}{2}$   |     |      |
|-------|----------------|---|-----|------|
|       |                | $ \stackrel{A2}{:} \leq \frac{(n-\omega)(n-\omega+1)}{2} $  |     |      |
|       |                | $ \begin{array}{c} A3 \\ \underline{(n-\omega)(n-\omega+1)}\\ 2 \end{array} $   |     |      |
|       |                | $ A4 \ge \frac{(n-\omega)(n-\omega-1)}{2} $   |     |      |
| Objec | ctive Question |   |     |      |
| 41    | 41             | Let $S = \left\{\frac{1}{n} : n \in N\right\} \cup \{0\}$ and $T = \left\{n + \frac{1}{n} : n \in N\right\}$ be the subsets of the metric space R with the usual metric. Then | 4.0 | 1.00 |
|       |                | A1 S is complete but not T:   |     |      |
|       |                | A2 T is complete but not S:   |     |      |
|       |                | A3 both S and T are complete  |     |      |
|       |                | A4 neither T nor S is complete  |     |      |
| Objec | ctive Question |   |     |      |
| 42    | 42             | $\int_{C} \frac{1}{2z+3} dz \text{ where C is }  z+3/2 =2 \text{ is}$   | 4.0 | 1.00 |
|       |                | $^{\mathrm{A1}}_{:}$ $^{2\pi\mathrm{i}}$  |     |      |
|       |                | A2 πi   |     |      |
|       |                | A3 <sub>0</sub>   |     |      |
|       |                | A4 1  |     |      |
| Objec | ctive Question |   |     |      |
| 43    | 43             | The radius of convergence of the power series $\sum_{n=0}^{\infty} \frac{(2n)!}{(n!)^2} (z-3i)^n$ is  | 4.0 | 1.00 |
|       |                | A1 <sub>1/4</sub> :   |     |      |
|       |                | A2 <sub>4</sub>   |     |      |
|       |                | A3 1  |     |      |

|       |                | A4 <sub>1/2</sub> :  |     |      |
|-------|----------------|--|-----|------|
|       |                |  |     |      |
|       | ctive Question |  |     |      |
| 44    | 44             | For the function $\frac{1}{(2\sin z - 1)^2}$   | 4.0 | 1.00 |
|       |                | Al z=0 is a simple pole  |     |      |
|       |                | A2 z=0 is a removable singularity  |     |      |
|       |                | $\frac{A3}{6} \frac{\pi}{6}$ is a pole of order 2  |     |      |
|       |                | $\frac{A4}{3}$ is a pole of order 2  |     |      |
|       | ctive Question |  |     |      |
| 45    | 45             | The range of a continuous real function defined on a connected space is  | 4.0 | 1.00 |
|       |                | A1 the real line   |     |      |
|       |                | A2 an Interval   |     |      |
|       |                | A3 a closed and bounded set  |     |      |
|       |                | A4<br>: compact  |     |      |
| Ohiec | ctive Question |  |     |      |
| 46    | 46             | Which of the following two spaces are homeomorphic:  | 4.0 | 1.00 |
|       |                | A1 [0,1] & (0,1)   |     |      |
|       |                | A2 [0,1] & {0} $\cup \left\{\frac{1}{n}: n \in N\right\}$  |     |      |
|       |                | A3 : $\{0\} \cup \left\{\frac{1}{n} : n \in N\right\} \& \left\{(x, y) \in \mathbb{R}^2 : x^2 + y^2 = 1\right\}$ |     |      |
|       |                | A4 (0,1) & $\{(x,y) \in \mathbb{R}^2 : x^2 + y^2 = 1\} - \{(1,0)\}$  |     |      |
| Ohiec | ctive Question |  |     |      |
| 47    | 47             | Which of the following points are collinear?   | 4.0 | 1.00 |
|       |                | A1 (0,0,-1), (0,1,0), (1,2,3)  |     |      |

|             |                | A2 (1,0,0), (0,1,0), (0,0,1)  |     |      |
|-------------|----------------|---|-----|------|
|             |                | A3 (5,3,-2), (3,2,1), (-1,0,7)  |     |      |
|             |                | A4 (1,2,0), (2,3,0), (2,2,2)  |     |      |
|             |                |   |     |      |
| Objec<br>48 | etive Question | The acute angle between the line joining the points $(3,1,-2)$ , $(4,0,-4)$ and $(4,-3,3)$ , $(6,-2,2)$ is  | 4.0 | 1.00 |
|             |                | The acute angle between the line joining the joining (3,1,-2), (4,0,-4) and (4,-3,3), (0,-2,2) is   |     |      |
|             |                | $\begin{array}{ccc} A1 & \underline{\pi} \\ \vdots & 3 \end{array}$   |     |      |
|             |                | $A2 \frac{\pi}{6}$  |     |      |
|             |                | A3 $\frac{\pi}{7}$  |     |      |
|             |                | $\begin{array}{cccccccccccccccccccccccccccccccccccc$  |     |      |
| Obiec       | ctive Question |   |     |      |
| 49          | 49             | The angle between the planes $2x-y+z=6$ and $x+y+2z=3$ is   | 4.0 | 1.00 |
|             |                | $\begin{array}{c c} A1 & \pi \\ \vdots & 3 \end{array}$   |     |      |
|             |                | $\begin{array}{ccc} A2 & \frac{\pi}{6} \\ \vdots & 6 \end{array}$   |     |      |
|             |                | A3 π/ <sub>2</sub> : 7  |     |      |
|             |                | $\begin{array}{ccc} A4 & \frac{\pi}{4} \\ \vdots & 4 \end{array}$   |     |      |
| Objec       | ctive Question |   |     |      |
| 50          | 50             | (i). If A is contained in the union of a collection of sets, then A is contained in a set in the collection.  (ii) If A contains an intersection of a collections of sets, then A contains a set in that collection | 4.0 | 1.00 |
|             |                | A1 Both (i) and (ii) are true   |     |      |
|             |                | A2 (i) is true but (ii) is not true   |     |      |
|             |                | A3 (ii) is true but (i) is not true   |     |      |
|             |                |   |     |      |
|             |                | A4 Neither (i) nor (ii) is true   |     |      |
| OIL:        | etive Question | A4 Neither (i) nor (ii) is true   |     |      |

|    |                | A1 A   |     |      |
|----|----------------|--|-----|------|
|    |                |  |     |      |
|    |                | A2 B   |     |      |
|    |                | A3 a finite nonempty set   |     |      |
|    |                | A4 some infinite set   |     |      |
|    | ctive Question |  |     |      |
| 52 | 52             | If $A = \{1,2,3\}$ and $B = \{2,4,6,8\}$ , then the number of functions from A to B is | 4.0 | 1.00 |
|    |                | A1 4C3   |     |      |
|    |                | A2 4p <sub>3</sub>   |     |      |
|    |                | A3 3 <sup>4</sup>  |     |      |
|    |                | A4 43 :  |     |      |
|    | ctive Question |  | 1   |      |
| 53 | 53             | Which is not a binary operator on Z  | 4.0 | 1.00 |
|    |                | $ \begin{array}{c} A1 \\ a * b = a \end{array} $                                       |     |      |
|    |                | A2 $a * b = max(a,b)$  |     |      |
|    |                | A3 a * b = average of a and b :  |     |      |
|    |                | A4 = a * b = a + 2b  |     |      |
|    | ctive Question |  |     |      |
| 54 | 54             | Greatest common divisor of two integers a, b with a less than or equal to b, is 1      | 4.0 | 1.00 |
|    |                | A1 only if both a and b are prime numbers  |     |      |
|    |                | A2 only if a and b have no common prime divisor  |     |      |
|    |                | A3 only if $a = b$   |     |      |
|    |                | A4 only if a does not divide b   |     |      |

| 55     | 55            | Let a prime factorization of an integer $n = p_1^{r_1} p_2^{r_2} \dots p_k^{r_k}$ is a square | 4.0 | 1.00 |
|--------|---------------|---|-----|------|
|        |               | 2172 7  |     |      |
|        |               | $\overset{\text{Al}}{:}$ if $r_1, r_2,, r_k$ are squares                                      |     |      |
|        |               | $^{\mathrm{A2}}_{:}$ if $r_1, r_2,, r_k$ are composite numbers                                |     |      |
|        |               | A3 if $r_1, r_2,, r_k$ are even integers  |     |      |
|        |               | $^{\mathrm{A4}}$ if the product of $r_1, r_2,, r_k$ is a square                               |     |      |
| Object | tive Question |   |     |      |
|        | 56            | The linear congruence ax = b(mod m) has a solution  | 4.0 | 1.00 |
|        |               | Al if a is a prime number:  |     |      |
|        |               | A2 if b is a prime number:  |     |      |
|        |               | A3 if a and b are prime numbers   |     |      |
|        |               | A4 if no integer greater than 1 divide both a and m.  |     |      |
| Object | tive Question |   |     |      |
|        | 57            | Let S denote the set of all functions from Z to Z. The composition of the functions is        | 4.0 | 1.00 |
|        |               | A1 not an associative binary operator :   |     |      |
|        |               | A2 not a commutative binary operator :  |     |      |
|        |               | A3 not a binary operator  |     |      |
|        |               | A4 not well defined :   |     |      |
| Object | tive Question |   |     |      |
|        | 58            | A permutation in a symmetric group $S_n$ is   | 4.0 | 1.00 |
|        |               | (i) a product of disjoint cycles. (ii) a product of disjoint transpositions.                  |     |      |
|        |               | A1 Both (i) and (ii) are true   |     |      |
|        |               | A2 (i) is true but (ii) is not true.  |     |      |
|        |               | A3 (ii) is true but (i) is not true.  |     |      |

|       |                | A4 Neither (i) nor (ii) is true.  |         |      |
|-------|----------------|---|---------|------|
| Ohiec | ctive Question |   | <u></u> |      |
| 59    | 59             | Let G be a group with identity element e. For some a, b in G then                             | 4.0     | 1.00 |
|       |                | (i) $ab = b$ then $a = e$   |         |      |
|       |                | (i) $ab = b$ then $a = e$<br>(ii) $a.a = e$ then $a = e$                                      |         |      |
|       |                | A1 Both (i) and (ii) are true   |         |      |
|       |                | A2 (i) is true but (ii) is not true.  |         |      |
|       |                | A3 (ii) is true but (i) is not true.  |         |      |
|       |                | A4 Neither (i) nor (ii) is true.  |         |      |
| Objec | ctive Question |   |         |      |
| 60    | 60             | Which one is a group  | 4.0     | 1.00 |
|       |                | A1 the set of integers modulo 6 with multiplication as binary operator :                      |         |      |
|       |                | A2 the set of integers modulo 6 without zero element with multiplication as binary operator : |         |      |
|       |                | A3 the set of 1,2,4,5,7,8 modulo 9 with multiplication as binary operator                     |         |      |
|       |                | A4 the set of 0,2,4 modulo 5 with addition as binary operator:                                |         |      |
| Objec | ctive Question |   |         |      |
| 61    | 61             | For every positive integer n  | 4.0     | 1.00 |
|       |                | A1 there exists a cyclic goup of order n  |         |      |
|       |                | A2 there exists a group of order n but there may not be any cyclic gorup of order n           |         |      |
|       |                | A3 there may not be any group of order n  |         |      |
|       |                | A4 there exists a group of order n if n is a prime.   |         |      |
| Objec | ctive Question |   |         |      |
| 62    | 62             | Let G be a cyclic group of order n where n > 2.   | 4.0     | 1.00 |
|       |                | Let G be a cyclic group of oracle it where it? 2.   |         |      |
|       |                | A1 Then G has unique generator.   |         |      |

|             |                | : Then G has unique generator if n is a prime number .  |     |      |
|-------------|----------------|---|-----|------|
|             |                | A3 Then G has exactly two generators.   |     |      |
|             |                | A4 Then G has atleast two generators.   |     |      |
|             |                |   |     |      |
| Objec<br>63 | etive Question | (i) A subgroup of a cyclic group is cyclic  | 4.0 | 1.00 |
| 05          |                | (ii) A nontrivial subgroup of an infinite cyclic group is infinite  |     | 1.00 |
|             |                | A1 Both (i) and (ii) are true.  |     |      |
|             |                | A2 (i) is true but (ii) is not true.  |     |      |
|             |                | A3 (ii) is true but (i) is not true.  |     |      |
|             |                | A4 Neither (i) nor (ii) is true.  |     |      |
| Objec       | ctive Question |   |     |      |
| 54          | 64             | Let G be a finite group and H be a subgroup of G. Which one of the statements is not true   | 4.0 | 1.00 |
|             |                | Al Any two left cosets of H in G have same number of elements   |     |      |
|             |                | A2 A left coset of H and a right coset of H has same number of elements:  |     |      |
|             |                | A3 Every left coset of H is equal to some right coset of H.   |     |      |
|             |                | A4 A left coset aH is equal to the left coset bH if a = bh for some h in H:   |     |      |
| Ohier       | ctive Question |   |     |      |
| 65          | 65             | Let G be a group of order n.  (i) For every divisor d of n there exists a subgroup of G with order d.  (ii) For every subgroup H of G the order of H is a divisor of n. | 4.0 | 1.00 |
|             |                | Al Both (i) and (ii) are true.  |     |      |
|             |                | A2 (i) is true but (ii) is not true.  |     |      |
|             |                | A3 (ii) is true but (i) is not true.  |     |      |
|             |                | A4 Neither (i) nor (ii) is true.  |     |      |
|             |                |   |     |      |

|             | Let G be a group. f and g are mappings from G to G defined as $f(a) = a^{-1}$ and $g(a) = a*a$ (i) f is a homomorphism (ii) g is a homomorphism |     |      |
|-------------|---|-----|------|
|             | A1 Both (i) and (ii) are true.  |     |      |
|             | A2 (i) is true but (ii) is not true.  |     |      |
|             | A3 (ii) is true but (i) is not true.  |     |      |
|             | A4 Neither (i) nor (ii) is true.  |     |      |
| Objective Q | lestion   |     |      |
| 67 67       | Let V be a finite dimensional vector space then a basis of V is a  (i) maximal linearly independent set  (ii) minimal generator set             | 4.0 | 1.00 |
|             | A1 Both (i) and (ii) are true.  |     |      |
|             | A2 (i) is true but (ii) is not true.  |     |      |
|             | A3 (ii) is true but (i) is not true.  |     |      |
|             | A4 Neither (i) nor (ii) is true.  |     |      |
| Objective Q | lection   |     |      |
| 68 68       | Which one is not a countable set?   | 4.0 | 1.00 |
|             | A1 The set of all positive rational numbers less than 1.  |     |      |
|             | A2 The set of positive irrational numbers less than 1.  |     |      |
|             | A3 The set of all positive rational numbers.  |     |      |
|             | A4 The set of all integers.   |     |      |
| Objective Q | estion  |     |      |
| 69 69       | The closed sets in real numbers is  | 4.0 | 1.00 |
|             | A1 a finite set :   |     |      |
|             | A2 a countable set :  |     |      |
|             | A3 a compact set  |     |      |

|             | II            |  | II  |      |
|-------------|---------------|--|-----|------|
|             |               | A4 is a set which may contain uncountable elements   |     |      |
| Obiec       | tive Question |  |     |      |
| 70          | 70            | (i) A countable infinite set of real numbers has a limit point (ii) A bounded infinite set of real numbers has a limit point   | 4.0 | 1.00 |
|             |               | A1 Both (i) and (ii) are true.   |     |      |
|             |               | A2 (i) is true but (ii) is not true.   |     |      |
|             |               | A3 (ii) is true but (i) is not true.   |     |      |
|             |               | A4 Neither (i) nor (ii) is true.   |     |      |
| Obiec       | tive Question |  |     |      |
| 71          | 71            | Let f be a continuous real valued function defined on real line Then which one is not a correct statement.   | 4.0 | 1.00 |
|             |               | A1: If U is open interval then f <sup>-1</sup> (U) is an open set.   |     |      |
|             |               | $\stackrel{A2}{:}$ If V is closed interval then $f^{-1}(V)$ is a closed set.   |     |      |
|             |               | A3 If U is open interval then f(U) is an open set.   |     |      |
|             |               | A4 f <sup>1</sup> need not be a continuous function.   |     |      |
| <b>N</b> .: | tive Question |  |     |      |
| 72          | 72            | If f is a real valued function defined on an open interval (a,b) and f is differentiable at x, a point in the interval, then which one of the following statements is correct? | 4.0 | 1.00 |
|             |               | A1 f is continuous at every point of (a,b).  |     |      |
|             |               | A2 f is continuous at x but need not be continuous at every point of (a,b).  |     |      |
|             |               | A3 f need not be continuous at x.  |     |      |
|             |               | A4 f is bounded on (a,b).  |     |      |
| Obiec       | tive Question |  |     |      |
| 73          | 73            | Lef f: $S \to T$ be a function and for every subset of A of S, $f^1(f(A)) = A$ if and only if  | 4.0 | 1.00 |
|             |               |  |     |      |

|       |               | A2 f is onto.  |     |      |
|-------|---------------|--|-----|------|
|       |               | A3 f is bijective.                                   |     |      |
|       |               | A4 f is identity map.                                |     |      |
| Objec | tive Question |  |     |      |
| 74    | 74            | A set of real numbers S has supremum if and only if  | 4.0 | 1.00 |
|       |               | A1 S is bounded.                                     |     |      |
|       |               | A2 S is bounded above.                               |     |      |
|       |               | A3 S is compact.                                     |     |      |
|       |               | A4 S is closed.                                      |     |      |
| Objec | tive Question |  |     |      |
| 75    | 75            | The constant sequence 1,1,1 is                       | 4.0 | 1.00 |
|       |               | A1 Convergent and the limit is 1                     |     |      |
|       |               | $^{\mathrm{A2}}$ divergent and the limit is $\infty$ |     |      |
|       |               | A3 convergent and the limit is 2                     |     |      |
|       |               | A4 none of these                                     |     |      |
| Objec | tive Question |  |     |      |
| 76    | 76            | The sequence $\left\{\frac{1}{n}\right\}$ is         | 4.0 | 1.00 |
|       |               | Al Convergent  |     |      |
|       |               | A2 divergent   |     |      |
|       |               | A3 unbounded:  |     |      |
|       |               | A4 none of these                                     |     |      |
|       | tive Question |  |     |      |
| Ohiec |               |  |     |      |

| space, then the whole space X and the empty set $ arphi $ are   | 4.0   | 1.00  |
|---|-------|-------|
|   | 4.0   | 1.00  |
|   | 4.0   | 1.00  |
|   | 4.0   | 1.00  |
|   | 4.0   | 1.00  |
|   |       | 1.00  |
|   |       |       |
|   |       |       |
|   |       |       |
|   |       |       |
|   |       |       |
|   |       |       |
| ng function is uniformly continuous on (0,1)  | 4.0   | 1.00  |
|   |       |       |
|   |       |       |
|   |       |       |
|   |       |       |
|   |       |       |
|   |       |       |
| ned by $f(x) = \begin{cases} 1 & \text{if } x \text{ is rational} \\ 0 & \text{if } x \text{ is irrational} \end{cases}$ is | 4.0   | 1.00  |
| ble   |       |       |
|   |       |       |
| tion  |       |       |
|   | nuous | ction |

|        |                | A4 Unbounded :  |     |      |
|--------|----------------|---|-----|------|
|        |                |   |     |      |
|        | etive Question |   | 4.0 | 1.00 |
| ,1     | O1             | The sequence of functions $f_n(x) = \frac{1}{1 + (x - n)^2}$ on $(-\infty, 0)$ is | 7.0 | 1.00 |
|        |                | A1 Pointwise Convergent   |     |      |
|        |                | A2 Uniformly Convergent   |     |      |
|        |                | A3 Divergent  |     |      |
|        |                | A4 Convergent   |     |      |
| Object | ctive Question |   |     |      |
|        | 82             | The sum $1 + \frac{1}{2} + \frac{1}{4} + =$                                       | 4.0 | 1.00 |
|        |                | A1 1 :  |     |      |
|        |                | A2 <sub>2</sub>   |     |      |
|        |                | A3  |     |      |
|        |                | A4 0  |     |      |
| Ohiec  | etive Question |   |     |      |
|        | 83             | $Lt_{n\to\infty} \frac{n^2}{2n^2 + 1} = ?$  | 4.0 | 1.00 |
|        |                | A1 2 :  |     |      |
|        |                | A2 1/2  |     |      |
|        |                | A3 0  |     |      |
|        |                | A4  |     |      |
| Object | ctive Question |   |     |      |
|        | 84             | In a metric space (X,d),  | 4.0 | 1.00 |
|        |                | A1 Every infinite set E has a limit point in E                                    |     |      |

|                   | A2 Every closed subset of a compact set is compact :  |     |      |
|-------------------|---|-----|------|
|                   | A3 Every closed and bounded set is compact  |     |      |
|                   | A4 Every subset of a compact set is closed:   |     |      |
| Objective Questio | n   |     |      |
| 85 85             | Let $f: X \to Y$ be any function between metric spaces, f is continuous if and only if for any open set $U \subseteq Y$ , | 4.0 | 1.00 |
|                   | $ \stackrel{\text{A1}}{:} f(U) \subseteq Y $  |     |      |
|                   | $\stackrel{\text{A2}}{:} f'(U) \subseteq Y$   |     |      |
|                   | $ \begin{array}{ccc} A3 & f'(U) \subseteq X \\ \vdots & & \end{array} $   |     |      |
|                   | A4 none of these  |     |      |
| Objective Questio | n   |     |      |
| 86 86             | The analytic function which maps the angular region $0 \leq \theta \leq \pi  /  4$  | 4.0 | 1.00 |
|                   | $\begin{bmatrix} A1 \\ \vdots \end{bmatrix}$ $Z^2$  |     |      |
|                   | A2 4z   |     |      |
|                   | $\begin{bmatrix} A3 \\ \vdots \end{bmatrix} Z^4$  |     |      |
|                   | A4 2 θ  |     |      |
| Objective Questio | n   |     |      |
| 87                | The integral of $\oint (z-z_0)^m dz$ is equal to  | 4.0 | 1.00 |
|                   | A1 : 0  for  m = -1   |     |      |
|                   | $^{A2}_{:}$ $2\pi i$ for $m = -1$   |     |      |
|                   | A3 : 2  for  m = -1   |     |      |
|                   |   |     |      |

| 88   88          | If an entire function $f(z)$ is bounded in absolute value for all $z$ , then –  | 4.0 | 1.00 |
|------------------|---|-----|------|
|                  | f(z) = constant   |     |      |
|                  | f(z) = zero   |     |      |
|                  | $f(z) = \infty$   |     |      |
|                  | A4 none of these  |     |      |
| Objective Questi | on  |     |      |
| 89 89            | If $f(z)$ is analytic in domain $D$ , then  | 4.0 | 1.00 |
|                  | $f^{(n)}(z)$ exist in $D$   |     |      |
|                  | $f^{(n)}(z)$ does not exist in $D$  |     |      |
|                  | A3 $f^{(\eta)}(z) = 0$ for all in D   |     |      |
|                  | A4 none of these  |     |      |
| Objective Questi |   |     |      |
| 90 90            | If $f(z)$ is continuous in a simple connected domain $D$ and if $\oint f(z)dz = 0$ for every closed contour in $D$ , then $-$ | 4.0 | 1.00 |
|                  | $f = \int_{\mathbb{R}}^{A_1} f (z)$ is non – analytic in $D$  |     |      |
|                  | f(z) is analytic in $D$   |     |      |
|                  | f(z) is constant  |     |      |
|                  | f(z) is bounded   |     |      |
| Objective Questi | on  |     |      |
| 91 91            | If $f(z)$ is entire function the Taylor series is   | 4.0 | 1.00 |
|                  | A1 Convergent for all z   |     |      |
|                  |   |     |      |
|                  | A2 Divergent for all z  |     |      |

|        |                | A4 Constant :   |     |      |
|--------|----------------|---|-----|------|
| Object | ctive Question |   |     |      |
| 92     | 92             | The residue of the function $f(z) = \frac{z^2}{(z-1)^2(z-2)}$ at $z=-2$   | 4.0 | 1.00 |
|        |                | A1 9/4<br>:   |     |      |
|        |                | A2 3/2  |     |      |
|        |                | A3 <sub>4/9</sub>   |     |      |
|        |                | A4 2/3  |     |      |
| Objec  | ctive Question |   |     |      |
| 93     | 93             | If $\omega$ be an imaginary cube root of unity then $(1 - \omega + \omega^2)^5 + (1 + \omega - \omega^2)^5$ is        | 4.0 | 1.00 |
|        |                | A1 64   |     |      |
|        |                | A2 32   |     |      |
|        |                | A3 16   |     |      |
|        |                | A4 8 :  |     |      |
| Obiec  | ctive Question |   |     |      |
| 94     | 94             | The value of $arg(z)+arg(\bar{z})$ , where z is not equal to zero is  | 4.0 | 1.00 |
|        |                | A1 0  |     |      |
|        |                | A2 π  |     |      |
|        |                | $\begin{array}{ccc} A3 & \frac{\pi}{2} \\ \vdots & 2 \end{array}$   |     |      |
|        |                | $\begin{array}{cccccccccccccccccccccccccccccccccccc$  |     |      |
| Objec  | ctive Question |   |     |      |
| 95     | 95             | If G is a region and f is non constant analytic function on G. The open mapping theorem state for any open set U in G | 4.0 | 1.00 |
|        |                | Al f(U) is closed:  |     |      |
|        |                |   |     |      |

| 96 96              | If z=a is an isolated singularity of f and $f(z) = \sum_{n=-\infty}^{\infty} a_n (z-a)^n$ is its Laurent series expansion in annulus (a;0;R) then if $a_n = 0$ for n<-1, we say | 4.0 | 1.00 |
|--------------------|---|-----|------|
|                    | Z=a is  |     |      |
|                    | Al A pole of order n  |     |      |
|                    | A2 A simple pole  |     |      |
|                    | A3 A removable singularity:   |     |      |
|                    | A4 An essential singularity   |     |      |
| Objective Question |   | 4.0 | 1.00 |
| 97                 | If $z_1 \neq z_2 \neq z_3 \neq z_4$ in $C_{\infty}$ the cross ratio $(z_1, z_2, z_3, z_4)$ is a real number if $z_1, z_2, z_3, z_4$ lies on                                     | 4.0 | 1.00 |
|                    | A1 Triangle   |     |      |
|                    | A2 Parabola   |     |      |
|                    | A3 Circle   |     |      |
|                    | A4 Hyperbola  |     |      |
| Objective Question | 1   |     |      |
| 98 98              | The real part of $\exp(\exp(i\theta))$ is   | 4.0 | 1.00 |
|                    | $e^{\cos \theta}$   |     |      |
|                    | $\stackrel{A2}{:} e^{\cos\theta} \sin(\sin\theta)$  |     |      |
|                    | $\stackrel{A3}{:} e^{\cos\theta} \cos(\sin\theta)$  |     |      |
|                    |   |     |      |

| \\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\   | 4.0  | 1.00   |
|--|--|--|
| A open set G is simply connected if G is connected and                                       | 4.0  | 1.00   |
| Al Every curve in G is homotopic to zero   |  |  |
| A2 Every closed curve in G homotopic to zero   |  |  |
| A3 Every curve in G is non homotopic to zero   |  |  |
| A4 Every closed curve in G, G is non homotopic to zero                                       |  |  |
| Question   |  |  |
| If $f(z) = z^6 - 5z^4 + 10$ , find the number of zeros in the annulus region $2 <  z  < 3$ . | 4.0  | 1.00   |
| A1 3   |  |  |
| A2 6   |  |  |
| A3 <sub>2</sub>  |  |  |
| A4 <sub>0</sub>  |  |  |
|  | A2 Every closed curve in G homotopic to zero  A3 Every curve in G is non homotopic to zero  A4 Every closed curve in G, G is non homotopic to zero  If $f(z) = z^6 - 5z^4 + 10$ , find the number of zeros in the annulus region $2 <  z  < 3$ .  A1 3  A2 6  A3 2 | A1 Every curve in G is homotopic to zero  A2 Every closed curve in G homotopic to zero  A3 Every curve in G is non homotopic to zero  A4 Every closed curve in G, G is non homotopic to zero  If $f(z) = z^6 - 5z^4 + 10$ , find the number of zeros in the annulus region $2 <  z  < 3$ .  A1 3  A2 6  A3 2 |